Jieh Hsiang: Refutational Theorem Proving Using Term-Rewriting Systems, Artificial Intelligence, 25 (1985) 255–300.

From $\langle \vee, \wedge, ' \rangle$ to $\langle +, * \rangle$ and vice versa:

$$\begin{vmatrix} x \lor y = x + y + (x * y) \\ x \land y = x * y \\ x' = 1 + x \end{vmatrix} x + y = (x' \land y) \lor (x \land y')$$

Axioms for a Boolean Ring:

$$\begin{vmatrix} x+0 & = & x \\ x+(-x) & = & 0 \\ x+y & = & y+x \\ x+(y+z) & = & (x+y)+z \\ x*1 & = & x \\ x*x & = & x \\ (x+y)*z & = & (x*z)+(y*z) \\ x*(y*z) & = & (x*y)*z \\ x*y & = & y*x \\ x+x & = & 0$$

Canonical Term Rewriting System for a Boolean Algebra, modulo associativity and commutativity of + and *:

THEOREM. A boolean term is valid iff its irreducible expression is 1; unsatisfiable iff its irreducible expression is 0; and satisfiable but not valid iff its irreducible expression is neither 0 nor 1.

EXERCISE. Let us show that: $p \lor (p \land q) \leftrightarrow p$. Indeed, we have the following rewriting:

$$\begin{array}{ll} p\vee(p\wedge q)\leftrightarrow p & \Rightarrow (p*(p*q)+p+(p*q))+p+1 \Rightarrow \\ \Rightarrow ((p*q)+p+(p*q))+p+1 & \Rightarrow (0+p)+p+1 & \Rightarrow \\ \Rightarrow p+p+1 & \Rightarrow 0+1 & \Rightarrow \end{array}$$